# Why Are Nitrenes More Stable than Carbenes? An Ab Initio Study 

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#### Abstract

High level ab initio calculations find that nitrenes are more stable than carbenes, as indicated by the computed enthalpy differences of $25-26 \mathrm{kcal} / \mathrm{mol}$ between triplet phenylnitrene and the isomeric triplet pyridylcarbenes. More generally, the greater thermodynamic stability of nitrenes manifests itself in the finding that the $\mathrm{N}-\mathrm{H}$ bond dissociation energies (BDEs) of aminyl radicals are approximately $20 \mathrm{kcal} / \mathrm{mol}$ lower than the $\mathrm{C}-\mathrm{H}$ BDEs of analogous alkyl radicals. The greater thermodynamic stability of nitrenes, relative to carbenes, is attributed to the large amount of 2 s character in the orbital that is occupied by the lone pair of electrons in nitrenes.


Ab initio calculations have found that the ring expansion of singlet phenylcarbene $(\mathbf{P h C H})$ to $1,2,4,6$-cycloheptatetraene (CHT) ${ }^{1}$ is much more exothermic than the analogous ring expansion of singlet phenylnitrene ( $\mathbf{P h N}$ ) to 1 -aza-1,2,4,6cycloheptatetraene (ACHT). ${ }^{2}$ The former ring expansion reaction was computed to be exothermic by $16-20 \mathrm{kcal} / \mathrm{mol} ;{ }^{1}$ whereas, the latter was calculated to be nearly thermoneutral. ${ }^{2}$


The calculated reversibility of the latter reaction accounts for the experimental finding that 1 -aza-1,2,4,6-cycloheptatetraene gives triplet $\mathbf{P h N},{ }^{3}$ presumably via formation of singlet $\mathbf{P h N}$, followed by intersystem crossing.

Evidence was presented that the large difference in the exothermicities of the two ring expansion reactions is primarily due to a large difference in thermodynamic stabilities between singlet $\mathbf{P h C H}$ and singlet $\mathbf{P h N} .{ }^{2}$ Since the singlet-triplet splitting of $18 \mathrm{kcal} / \mathrm{mol}$ in $\mathbf{P h} \mathbf{N}^{4,5}$ is considerably greater than $\Delta E_{\mathrm{ST}} \approx 5 \mathrm{kcal} / \mathrm{mol}$ in $\mathbf{P h C H},{ }^{1,6,7}$ the difference between the

[^0]thermodynamic stabilities of the triplets is ca. $13 \mathrm{kcal} / \mathrm{mol}$ larger than that between the singlets. Wentrup and Platz have each suggested that a large difference between the thermodynamic stabilities of the triplets is the origin of the much lower reactivity of triplet $\mathbf{P h N}$, compared to triplet $\mathbf{P h C H} .{ }^{8}$ Wentrup and Platz also each proposed that the greater thermodynamic stability of triplet $\mathbf{P h N}$, relative to triplet $\mathbf{P h C H}$, is mirrored in the relative thermodynamic stabilities of triplet NH versus triplet $\mathrm{CH}_{2}$, as exemplified, for instance, by the lower bond dissociation energy (BDE) for forming triplet NH from ${ }^{\bullet} \mathrm{NH}_{2}$ than for forming triplet $\mathrm{CH}_{2}$ from ${ }^{\bullet} \mathrm{CH}_{3}$.

Since $\mathbf{P h C H}$ and $\mathbf{P h N}$ are not isomers, their energies cannot be compared directly. However, pyridylcarbenes (PyCH) are isomers of $\mathbf{P h N}$, and consistent with the rearrangement of the former to the latter, ${ }^{9}$ our calculations found that singlet $\mathbf{P h N}$ is much lower in energy than both singlet 2-PyCH ${ }^{2}$ and singlet 3-PyCH. ${ }^{10}$ In this paper, we have used 3-PyCH as a link



3-PyCH
between $\mathbf{P h C H}$ and $\mathbf{P h N},{ }^{11}$ so that we can make meaningful comparisons between the energies of the latter two molecules.
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(10) The lowest singlet state of $\mathbf{3 - P y C H}$ is calculated to be lower in energy than that of $\mathbf{2 - P y C H}{ }^{2}$ by $1.0 \mathrm{kcal} / \mathrm{mol}$ at $(8,8)$ CASSCF/6-31G* and by $2.0 \mathrm{kcal} / \mathrm{mol}$ at $(8,8)$ CASPT2N/6-31G*.

Table 1. Relative Energies and Enthalpies at CASSCF/6-31G* Optimized Geometries of Triplet 3-PyCH, Triplet PhN, and Pairs of Molecules Formed from Them by Addition of Hydrogen Atoms ${ }^{a}$

| calculation | 3-PyCH ${ }^{\text {b }}$ | $\mathbf{P h N H}_{2}$ | 3-PyCH ${ }^{\text {b }}$ | PhNH | 3-PyCH ${ }^{\text {b,c }}$ | PhN |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ${ }^{1} \mathrm{~A}^{\prime}$ | ${ }^{1} \mathrm{~A}^{\prime}$ | ${ }^{2} \mathrm{~A}^{\prime \prime}$ | ${ }^{2}$ A ${ }^{\prime \prime}$ | ${ }^{3} \mathrm{~A}^{\prime \prime}$ | ${ }^{3} \mathrm{~A}_{2}$ |
| ZPE | 77.0 | $+0.5{ }^{\text {d }}$ | 67.6 | $+0.8{ }^{\text {d }}$ | 59.6 | $+0.5^{d}$ |
| $C_{\mathrm{v}} \times 298 \mathrm{~K}$ | 6.3 | $+0.3{ }^{d}$ | 6.3 | $-0.2^{\text {d }}$ | 6.1 | $-0.2^{\text {d }}$ |
| CASSCF/6-31G* | -285.80990 | $+5.7^{\text {e }}$ | -285.19124 | $-1.9{ }^{\text {e }}$ | -284.55070 | $-27.8^{e}$ |
| CASPT2N/6-31G* | -286.68371 | $+1.9{ }^{\text {e }}$ | -286.04787 | $-1.5{ }^{\text {e }}$ | -285.38350 | $-26.4{ }^{e}$ |
| BVWN5/cc-pVDZ | -289.02535 | $-0.9{ }^{\text {e }}$ | -288.35937 | $-2.2{ }^{\text {e }}$ | -287.65819 | $-25.5{ }^{\text {e }}$ |
| BVWN5/AUG-cc-pVTZ | -289.12245 | $-3.2{ }^{e}$ | -288.45363 | $-3.3^{e}$ | -287.74861 | $-25.3{ }^{\text {e }}$ |

${ }^{a}$ The electrons correlated in the CASSCF calculations consisted of the $\pi$ plus the unpaired $\sigma$ electrons. ${ }^{b}$ Absolute energies in hartrees, unscaled CASSCF/6-31G* zero-point energies (ZPEs) and heat capacities in kcal/mol. ${ }^{c}$ Energies and enthalpies are for the syn conformer. ${ }^{d}$ Relative energy in $\mathrm{kcal} / \mathrm{mol}$. ${ }^{e}$ Relative energy has been converted to an enthalpy difference by correcting for $\Delta Z P E$ and $\Delta C_{\mathrm{v}} \times 298 \mathrm{~K}$.

Comparing the lowest singlet states of $\mathbf{P h C H}$ and $\mathbf{P h N}$ is complicated by the fact that they have different orbital occupancies. In ${ }^{1} \mathrm{~A}^{\prime} \mathbf{P h C H}$, two electrons occupy the hybridized, $\sigma$, nonbonding orbital on carbon; ${ }^{1,7}$ whereas, in ${ }^{1} \mathrm{~A}_{2} \mathbf{P h N}$, only one electron occupies the pure $2 \mathrm{p}, \sigma$, nonbonding orbital on nitrogen. ${ }^{2,5}$ However, the lowest triplet states ( ${ }^{3} \mathrm{~A}^{\prime \prime}$ in $\mathbf{P h C H}$ and ${ }^{3} \mathrm{~A}_{2}$ in $\mathbf{P h N}$ ) each have one unpaired electron in a nonbonding $\sigma$ orbital and one in a nonbonding $\pi$ MO. This makes comparison of the triplet ground states of $\mathbf{P h C H}$ and PhN much easier, both conceptually and computationally, ${ }^{12}$ than comparison of their singlet states.

The results of our calculations on triplet PhCH and triplet PhN support the conjecture ${ }^{8}$ that the latter is less reactive than the former because the $\mathrm{N}-\mathrm{H}$ BDE in anilinyl radical ( $\mathbf{P h N H )}$ is much smaller than the $\mathrm{C}-\mathrm{H}$ BDE in benzyl radical $\left(\mathbf{P h C H}_{\mathbf{2}}\right)$. Our calculations also provide an explanation for this large difference in BDEs.

## Computational Methods

Geometry optimizations were performed using complete active space (CAS) SCF calculations with the $6-31 G^{*}$ basis set. ${ }^{13}$ In each case, the electrons correlated in the CASSCF calculations consisted of all of the $\pi$ plus the unpaired $\sigma$ electrons. CASSCF/6-31G* frequency calculations confirmed that the stationary points found were minima, and the calculations also provided unscaled, zero-point energy (ZPE) corrections.

Only real vibrational frequencies were found for all molecules, except for the $D_{3 h}$ methyl radical. At the ROHF level of theory, it showed one imaginary frequency, correspondng to an out-of-plane distortion; an ROHF geometry reoptimization provided an energy minimum with $C_{3 v}$ symmetry and an energy $0.03 \mathrm{kcal} / \mathrm{mol}$ lower than that at the $D_{3 h}$ geometry. However, the $C_{3 v}$ geometry was found to be higher in energy than the $D_{3 h}$ geometry at correlated levels of theory; thus, we have reported single-point energies at the $D_{3 h}$ geometry. The zero-point vibrational energy for $D_{3 h}$ methyl radical was taken from UHF/6-31G* calculations, which find this geometry to be an energy minimum.

Second-order Møller-Plesset theory was used to provide dynamic correlation beyond the CASSCF level via CASPT2N ${ }^{14}$ calculations, which were performed at the CASSCF/6-31G*-optimized geometries. For species lacking the large phenyl and pyridyl substituents, G2 enthalpies ${ }^{15}$ were also computed.

Single-point density functional theory (DFT) calculations were carried out at CASSCF/6-31G* optimized geometries, using Becke's 1988 exchange functional ${ }^{16}$ and Vosko, Wilk, and Nusair's correlation functional V. ${ }^{17}$ This method is designated as BVWN5. Recent calculations by Squires and co-workers have found that BVWN5 energies are in good agreement with experimental measures of both $\Delta E_{\mathrm{ST}}$ and "carbene stabilization energy" for phenylcarbene. ${ }^{18}$ Two different correlation-consistent basis sets ${ }^{19}$ were used in the DFT calculations, a polarized valence double- $\zeta$ basis set and a polarized valence triple- $\zeta$ basis set that was augmented with diffuse functions ( $s, p$, and $d$ on hydrogen; $s, p, d$, and $f$ on carbon and nitrogen). These basis sets are designated as cc-pVDZ and AUG-cc-pVTZ, respectively.

CASPT2N calculations were performed using MOLCAS-3. ${ }^{20}$ All other calculations were carried out using Gaussian 94. ${ }^{21}$ Optimized geometries and single-point energies are available as Supporting Information.

## Results and Discussion

As shown in Table 1, triplet $\mathbf{P h N}$ is calculated to be 25-26 $\mathrm{kcal} / \mathrm{mol}$ lower in enthalpy than triplet 3-PyCH ${ }^{22}$ at the CASPT2N/6-31G* and BVWN5/AUG-cc-pVTZ levels of theory. Table 1 also shows that the corresponding radicals, PhNH and 3-PyCH 2 , differ in enthalpy by only $1-3 \mathrm{kcal} / \mathrm{mol}$. Therefore, the large enthalpy difference between $\mathbf{P h N}$ and $\mathbf{3 - P y C H}$ must reflect an intrinsic enthalpy difference between arylnitrenes and arylcarbenes, rather than a difference between the abilities of the phenyl and pyridyl groups to stabilize an unpaired $\pi$ electron. In fact, our calculations find that the rotation barriers for the
(11) 3-PyCH was chosen over 2-PyCH for detailed study because the interaction between the ring nitrogen and the divalent carbon atom is smaller in the former carbene than in the latter. For example, whereas, at the CASPT2N level, the syn and anti geometries differ in energy by only 0.3 $\mathrm{kcal} / \mathrm{mol}$ in singlet 3-PyCH , they differ by $3.6 \mathrm{kcal} / \mathrm{mol}$ in singlet 2-PyCH. The greater similarity in energies of the syn and anti conformers of 3-PyCH, compared to 2-PyCH, thus makes 3-PyCH a better model for $\mathbf{P h C H}$, for which the analogous conformers are degenerate.
(12) For example, CASPT2N/6-31G* calculations give a singlet-triplet splitting that is too large by almost $10 \mathrm{kcal} / \mathrm{mol}$ for $\mathbf{P h C H},{ }^{1 \mathrm{c}}$ but that is very close to experiment for $\mathbf{P h} \mathbf{N}^{2,4}$ These findings indicate that CASPT2N gives much more accurate results for electronic states with the same type of orbital occupancy (e.g., the ${ }^{1} \mathrm{~A}_{2}$ and ${ }^{3} \mathrm{~A}_{2}$ states of $\mathbf{P h N}$ ) than with different orbital occupancies (e.g., the ${ }^{1} \mathrm{~A}^{\prime}$ and ${ }^{3} \mathrm{~A}^{\prime \prime}$ states of $\mathbf{P h C H}$ ).
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(22) Since the energy of syn-3-PyCH is lower than that of the anti-3$\mathbf{P y C H}$ in both the lowest singlet and triplet states, the energies computed for the syn stereoisomer are those that are reported in Table 1.

Table 2. $\mathrm{BDE}\left(\mathrm{DH}_{298}\right.$ in $\left.\mathrm{kcal} / \mathrm{mol}\right)$ of $\mathrm{RNH}_{2}$, Relative to $\mathrm{R}^{\prime} \mathrm{CH}_{3}$, [ $\Delta H(1)$ ] at CASSCF/6-31G* Optimized Geometries ${ }^{a}$

| substituents/calculation | $\Delta H(1)$ |
| :---: | :---: |
| $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{H}^{b}$ |  |
| $\triangle \mathrm{ZPE}$ | $+0.3$ |
| $\Delta C_{\mathrm{v}} \times 298 \mathrm{~K}$ | -0.5 |
| $\mathrm{R}(\mathrm{O}) \mathrm{HF}^{c} / 6-31 \mathrm{G}^{*}$ | -6.2 |
| CASPT2N ${ }^{d} / 6-31 \mathrm{G}^{*}$ | -1.3 |
| BVWN5/cc-pVDZ | -1.1 |
| BVWN5/AUG-cc-pVTZ | 1.4 |
| G2 | 2.1 |
| exptl $\Delta D H_{298}{ }^{e}$ | 3.7 |
| $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{Ph}^{f}$ |  |
| $\triangle \mathrm{ZPE}$ | +0.2 |
| $\Delta C_{\mathrm{v}} \times 298 \mathrm{~K}$ | -0.5 |
| CASSCF/6-31G* | -7.3 |
| CASPT2N/6-31G* | -3.0 |
| BVWN5/cc-pVDZ | -1.0 |
| BVWN5/AUG-cc-pVTZ | 0.3 |
| $\mathrm{R}=\mathrm{Ph}, \mathrm{R}^{\prime}=3-\mathrm{Py}{ }^{f}$ |  |
| $\triangle \mathrm{ZPE}$ | +0.3 |
| $\Delta C_{\mathrm{v}} \times 298 \mathrm{~K}$ | -0.5 |
| CASSCF/6-31G* | -7.6 |
| CASPT2N/6-31G* | -3.4 |
| BVWN5/cc-pVDZ | -1.3 |
| BVWN5/AUG-cc-pVTZ | -0.1 |

${ }^{a}$ The electrons correlated in the CASSCF calculations consisted of the $\pi$ plus the unpaired $\sigma$ electrons. ${ }^{b}$ Enthalpies for eq 1 include differences in zero-point energies ( $\triangle Z \mathrm{PE}$ ) and heat capacities at 298 $\mathrm{K}\left(\Delta C_{\mathrm{v}} \times 298 \mathrm{~K}\right)$, obtained from calculations at the $\mathrm{R}(\mathrm{O}) \mathrm{HF} / 6-31 \mathrm{G}^{*}$ level of theory. ${ }^{c}$ RHF for $\mathrm{RNH}_{2}$ and $\mathrm{R}^{\prime} \mathrm{CH}_{3}$; ROHF for RNH and $\mathrm{R}^{\prime} \mathrm{CH}_{2} .{ }^{d}$ Using $\mathrm{R}(\mathrm{O}) \mathrm{HF}$ reference wave functions. ${ }^{e}$ Values are averages in $\mathrm{kcal} / \mathrm{mol}$ from ref 26. ${ }^{f}$ Enthalpies for eq 1 include differences in zero-point energies ( $\triangle Z \mathrm{PE}$ ) and heat capacities at $298 \mathrm{~K}\left(\Delta C_{\mathrm{v}} \times 298\right.$ K ), obtained from calculations at the CASSCF/6-31G* level of theory.
methylene groups in $\mathbf{P h C H}_{\mathbf{2}}$ and $\mathbf{3}-\mathbf{P y C H}_{\mathbf{2}}$ differ by only 0.3 $\mathrm{kcal} / \mathrm{mol}$ at the CASSCF/6-31G* level of theory, confirming that phenyl and 3-pyridyl do, indeed, provide comparable stabilization for an unpaired $\pi$ electron.

Since our calculations find that, like $\mathbf{P h N H}$ and $\mathbf{3 - P y C H} \mathbf{2}$, $\mathbf{P h N H}_{\mathbf{2}}$ and $\mathbf{3}-\mathbf{P y C H}_{\mathbf{3}}$ have very similar enthalpies, the data in Table 1 imply that the $\mathrm{N}-\mathrm{H}$ BDE of $\mathbf{P h N H}_{\mathbf{2}}$ and $\mathrm{C}-\mathrm{H}$ BDE of $\mathbf{3}-\mathrm{PyCH}_{3}$ are quite similar. The reaction in eq 1 can be used to demonstrate that this is, in fact, the case not only for $\mathrm{R}=\mathrm{Ph}$ and $\mathrm{R}^{\prime}=3$-Py but also for $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{Ph}$ and for $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{H}$. The enthalpies calculated for this reaction at different levels of theory are given in Table 2.


As shown in Table 2, the computed differences [ $\Delta H(1)$ in eq 1] between the BDEs $\left(\mathrm{DH}_{298}\right)$ depend somewhat on the level of theory used. However, for $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{H}$, BVWN5/AUG-cc-pVTZ gives essentially the same value for $\Delta H(1)$ as the G2 calculations, and the G2 enthalpy for the reaction in eq 1 is within $2 \mathrm{kcal} / \mathrm{mol}$ of the experimental difference between the BDEs of $\mathrm{NH}_{3}$ and $\mathrm{CH}_{4}$. For all three sets of R and $\mathrm{R}^{\prime}$, CASPT2N/6-31G* gives values for $\Delta H(1)$ that are ca. $3 \mathrm{kcal} /$ mol lower than those computed with BVWN5/AUG-cc-pVTZ.

The computed differences between the BDEs also depend somewhat on the substituents, R and $\mathrm{R}^{\prime}$. For example, with R $=\mathrm{R}^{\prime}=\mathrm{Ph}, \Delta H(1)$ is calculated to be up to $2 \mathrm{kcal} / \mathrm{mol}$ smaller than that for $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{H}$. Nevertheless, regardless of the set of substituents or of the level of theory used, the results in Table 2 show that the $N-H$ BDEs of primary amines are nearly the

Table 3. $\mathrm{BDE}\left(\mathrm{DH}_{298}\right.$ in $\left.\mathrm{kcal} / \mathrm{mol}\right)$ of RNH , Relative to $\mathrm{R}^{\prime} \mathrm{CH}_{2}$, [ $\Delta H(2)$ ] at CASSCF/6-31G* Optimized Geometries ${ }^{a}$

| substituents/calculation | $\Delta H(2)$ |
| :---: | :---: |
| $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{H}^{b}$ |  |
| $\triangle \mathrm{ZPE}$ | -0.1 |
| $\Delta C_{\mathrm{v}} \times 298 \mathrm{~K}$ | +0.2 |
| ROHF/6-31G* | -23.2 |
| CASPT2N ${ }^{c} / 6-31 \mathrm{G}^{*}$ | -21.9 |
| BVWN5/cc-pVDZ | -19.3 |
| BVWN5/AUG-cc-pVTZ | -17.5 |
| G2 | -18.4 |
| exptl $\Delta D H_{298}{ }^{\text {d }}$ | -18.7 |
| $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{Ph}^{e}$ |  |
| $\triangle \mathrm{ZPE}$ | -0.2 |
| $\Delta C_{\mathrm{V}} \times 298 \mathrm{~K}$ | +0.1 |
| CASSCF/6-31G* | -25.6 |
| CASPT2N/6-31G* | -24.7 |
| BVWN5/cc-pVDZ | -23.7 |
| BVWN5/AUG-cc-pVTZ | -22.5 |
| $\mathrm{R}=\mathrm{Ph}, \mathrm{R}^{\prime}=3-\mathrm{Py}^{e}$ |  |
| $\triangle \mathrm{ZPE}$ | -0.2 |
| $\Delta C_{\mathrm{v}} \times 298 \mathrm{~K}$ | +0.1 |
| CASSCF/6-31G* | -25.8 |
| CASPT2N/6-31G* | -24.8 |
| BVWN5/cc-pVDZ | -23.2 |
| BVWN5/AUG-cc-pVTZ | -21.9 |

${ }^{a}$ The electrons correlated in the CASSCF calculations consisted of the $\pi$ plus the unpaired $\sigma$ electrons. ${ }^{b}$ Enthalpies for eq 2 include differences in zero-point energies ( $\triangle Z \mathrm{ZPE}$ ) and heat capacities at 298 $\mathrm{K}\left(\Delta C_{\mathrm{v}} \times 298 \mathrm{~K}\right)$, obtained from calculations at the ROHF/6-31G* level of theory. ${ }^{c}$ Using ROHF reference wave functions. ${ }^{d}$ Values are averages in $\mathrm{kcal} / \mathrm{mol}$ from ref $26 .{ }^{e}$ Enthalpies for eq 2 include differences in zero-point energies ( $\triangle Z \mathrm{ZPE}$ ) and heat capacities at 298 $\mathrm{K}\left(\Delta C_{\mathrm{v}} \times 298 \mathrm{~K}\right)$, obtained from calculations at the CASSCF/6-31G* level of theory.
same as the $C-H$ BDEs of the analogous primary alkanes, despite the greater electronegativity of nitrogen compared to carbon.

In contrast, the much lower enthalpy computed for triplet PhN, compared to triplet 3-PyCH, implies that the $\mathrm{N}-\mathrm{H}$ BDE of $\mathbf{P h N H}$ radical is much reduced from the $\mathrm{C}-\mathrm{H}$ BDE of $\mathbf{3}-\mathbf{P y C H}_{2}$ radical. The reaction in eq 2 can be used to demonstrate that the $\mathrm{N}-\mathrm{H}$ BDE of RNH is lower than the $\mathrm{C}-\mathrm{H}$ BDE of $\mathrm{R}^{\prime} \mathrm{CH}_{2}$, not only for $\mathrm{R}=\mathrm{Ph}$ and $\mathrm{R}^{\prime}=3$-Py but also for $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{Ph}$ and for $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{H}$. The enthalpies calculated

for this reaction are given in Table 3. They indicate that triplet nitrenes are, in general, much more thermodynamically stable than the analogous triplet carbenes.

The enthalpies in Table 3 for the reaction in eq 2 show small variations with levels of theory and substituents, R and $\mathrm{R}^{\prime}$, which are very similar to those seen in Table 2 for the reaction in eq 1. For $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{H}$, the BVWN5/AUG-cc-pVTZ and G 2 values for $\Delta H(2)$ are, like those for $\Delta H(1)$, within $1 \mathrm{kcal} / \mathrm{mol}$ of each other, and these enthalpy changes are essentially the same as the differences between the experimental heats of formation of the molecules in eq 2. For all three sets of substituents, CASPT2N/6-31G* gives values of $\Delta H(2)$ that are again ca. 3 $\mathrm{kcal} / \mathrm{mol}$ lower than those computed with BVWN5/AUG-ccpVTZ , and like $\Delta H(1), \Delta H(2)$ is calculated to be $2-5 \mathrm{kcal} /$ mol more negative for $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{Ph}$ than for $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{H}$.

Despite these small variations with the substituents, $R$ and $\mathrm{R}^{\prime}$, and with the level of theory used, the results in Table 3 show that the $\mathrm{N}-\mathrm{H}$ BDE of an aminyl radical to form a triplet
nitrene is much lower than the $\mathrm{C}-\mathrm{H}$ BDE of a comparable primary alkyl radical to form a triplet carbene. Since the much lower $\mathrm{N}-\mathrm{H}$ BDE of $\mathbf{P h N H}$, compared to the $\mathrm{C}-\mathrm{H}$ BDE of 3- $\mathbf{P y C H}_{2}$, can be rigorously attributed to the much lower enthalpy of the triplet nitrene, relative to the triplet carbene, the results in Table 3 establish that, in general, triplet nitrenes are ca. $20 \mathrm{kcal} / \mathrm{mol}$ more thermodynamically stable than comparably substituted triplet carbenes.

These computational results confirm the suggestions of Wentrup and Platz that (a) the relative lack of reactivity and the greater selectivity found for triplet $\mathbf{P h N}$, compared to triplet $\mathbf{P h C H}$, has a thermodynamic origin and (b) this difference between the thermodynamic stabilities of $\mathbf{P h N}$ and $\mathbf{P h C H}$ is but one example of a more general difference between the thermodynamic stabilities of nitrenes and carbenes, which is also seen in the difference between the $\mathrm{N}-\mathrm{H}$ BDE in ${ }^{\circ} \mathrm{NH}_{2}$ and the $\mathrm{C}-\mathrm{H} \mathrm{BDE}$ in ${ }^{\circ} \mathrm{CH}_{3} .{ }^{8}$

Despite the ca. $13 \mathrm{kcal} / \mathrm{mol}$ larger value of $\Delta E_{\mathrm{ST}}$ in $\mathbf{P h} \mathbf{N}^{2,4,5}$ than in $\mathbf{P h C H},{ }^{1,6,7}$ the even larger difference between the thermodynamic stabilities of triplet $\mathbf{P h N}$ and triplet $\mathbf{P h C H}$ results in singlet $\mathbf{P h N}$ also being predicted to be considerably more thermodynamically stable than singlet $\mathbf{P h C H} .{ }^{23}$ The greater thermodynamic stability of $\mathbf{P h N}$ accounts for the calculated differences between the overall energetics of the ring expansions of singlet $\mathbf{P h N}$ and $\mathbf{P h C H}{ }^{2}$. Whereas ring expansion of singlet $\mathbf{P h C H}$ to CHT is computed to be very exothermic, ${ }^{1}$ that of singlet PhN to ACHT is calculated to be nearly thermoneutral. ${ }^{2,24}$ As noted in the Introduction, experimental evidence indicates that ring expansion of singlet $\mathbf{P h N}$ is, in fact, reversible. ${ }^{3}$

The explanation of why nitrenes are thermodynamically more stable than carbenes must be the same as the reason the $\mathrm{N}-\mathrm{H}$ BDE in RNH is much smaller than the $\mathrm{C}-\mathrm{H}$ BDE in $\mathrm{RCH}_{2}$. Part of the reason for this difference in BDEs could be the difference in hybridization of the $\mathrm{X}-\mathrm{H}$ bonds that are broken in the two radicals. For example, for $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{H}$, the CISD/ $6-311 \mathrm{G}(2 \mathrm{~d}, \mathrm{p})$-optimized bond angle in ${ }^{\circ} \mathrm{NH}_{2}$ is $102.6^{\circ}$; whereas, the $\mathrm{H}-\mathrm{C}-\mathrm{H}$ bond angles in ${ }^{\circ} \mathrm{CH}_{3}$ are $120.0^{\circ}$. Comparison of these bond angles indicates that the $\mathrm{N}-\mathrm{H}$ bonds in ${ }^{-} \mathrm{NH}_{2}$ have less 2 s character than the $\mathrm{C}-\mathrm{H}$ bonds in ${ }^{\circ} \mathrm{CH}_{3}$, and this difference in hybridization could account for at least some of the difference between the BDEs in these two radicals.

An estimate of the size of this effect was obtained by constraining one of the $\mathrm{H}-\mathrm{C}-\mathrm{H}$ bond angles in ${ }^{\circ} \mathrm{CH}_{3}$ to the $\mathrm{H}-\mathrm{N}-\mathrm{H}$ bond angle of $102.6^{\circ}$ in ${ }^{\circ} \mathrm{NH}_{2}$ and comparing the BDE of one of the $\mathrm{C}-\mathrm{H}$ bonds, thus constrained, to that of one of the unconstrained $\mathrm{C}-\mathrm{H}$ bonds in ${ }^{\bullet} \mathrm{CH}_{3}$. To maintain as closely as possible the same hybridization in each of the two triplet methylenes as in the methyl radical from which it was formed, the $\mathrm{H}-\mathrm{C}-\mathrm{H}$ bond angle was frozen at a value of $128.7^{\circ}$ in one triplet methylene and at $120.0^{\circ}$ in the other. The resulting

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Figure 1. $\mathrm{R}(\mathrm{O}) \mathrm{HF} / 6-311 \mathrm{G}(2 \mathrm{~d}, \mathrm{p}) \mathrm{MO}$ energies (hartrees) for $\mathrm{NH}_{3}$, $\cdot \mathrm{NH}_{2}$, and triplet NH .
isodesmic reaction, which probes the effect of hybridization on the BDE of methyl radical, is given in eq 3 .


The geometry constraints in eq 3 make ${ }^{\bullet} \mathrm{CH}_{3}$ and triplet $\mathrm{CH}_{2}$ each higher in energy on the left-hand side of this equation than on the right. Nevertheless, the CISD/6-311G(2d,p) energy of $\Delta E(3)=-4.5 \mathrm{kcal} / \mathrm{mol}$ is $16.3 \mathrm{kcal} / \mathrm{mol}$ smaller in size than that of $\Delta E=-20.8 \mathrm{kcal} / \mathrm{mol}$ for the reaction in eq 2 at the same level of theory for $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{H}$. Therefore, the difference in hybridization between ${ }^{\bullet} \mathrm{NH}_{2}$ and ${ }^{\bullet} \mathrm{CH}_{3}$ probably accounts for less than a quarter of the difference between the BDEs in eq 2 for $R=R^{\prime}=H$.

If the difference in hybridization of the bonds being broken accounts for only a small fraction of the difference between the BDEs of $\cdot \mathrm{NH}_{2}$ and ${ }^{\bullet} \mathrm{CH}_{3}$, the major contributor to the difference between these BDEs must reside in the changes in hybridization that accompany formation of triplet NH and triplet $\mathrm{CH}_{2} .{ }^{25}$ Loss of $\mathrm{H}^{\bullet}$ from both ${ }^{\bullet} \mathrm{NH}_{2}$ and ${ }^{\bullet} \mathrm{CH}_{3}$ allows the 2 s character in the remaining doubly occupied $\sigma$ orbitals to increase. These increases are evident in (a) the loss of all 2 s character from the $\sigma$ orbital that becomes singly occupied on going from ${ }^{\circ} \mathrm{NH}_{2}$ to triplet NH and (b) the opening of the $\mathrm{H}-\mathrm{C}-\mathrm{H}$ angle on going from ${ }^{\circ} \mathrm{CH}_{3}\left(\mathrm{H}-\mathrm{C}-\mathrm{H}=120^{\circ}\right)$ to triplet $\mathrm{CH}_{2}\left(\mathrm{H}-\mathrm{C}-\mathrm{H}=132.5^{\circ}\right.$ at the CISD/6-311G(2d,p) level of theory). However, the electrons in the lone pair orbital of triplet NH benefit from rehybridization more than those in the $\mathrm{C}-\mathrm{H}$ bonding orbitals of triplet $\mathrm{CH}_{2}$ (or in the $\mathrm{N}-\mathrm{H}$ bonding orbital of triplet NH), because the lone pair of electrons in NH is localized almost entirely on N ; whereas, the pair of electrons in each $\mathrm{C}-\mathrm{H}$ bond of $\mathrm{CH}_{2}$ is shared between carbon and hydrogen.

Figure 1 gives the $\mathrm{R}(\mathrm{O}) \mathrm{HF} / 6-311 \mathrm{G}(2 \mathrm{~d}, \mathrm{p})$ orbital energies for $\mathrm{NH}_{3},{ }^{\bullet} \mathrm{NH}_{2}$, and triplet NH. It shows graphically the decrease

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Figure 2. Schematic depiction of the ${ }^{3} \Sigma^{-} \rightarrow{ }^{3} \Pi$ excitation in NH and the ${ }^{2} \mathrm{~B}_{1} \rightarrow{ }^{2} \mathrm{~A}_{1}$ excitation in ${ }^{\circ} \mathrm{NH}_{2}$.
in the energy of the lone pair orbital on going from ${ }^{\circ} \mathrm{NH}_{2}$ to triplet NH. The energy of the lone pair orbital drops by 38 $\mathrm{kcal} / \mathrm{mol}$.

The extent to which rehybridization stabilizes the lone pair orbital in triplet NH can be independently assessed by comparing the vertical ${ }^{3} \Sigma^{-} \rightarrow{ }^{3} \Pi$ excitation energy in NH with the vertical ${ }^{2} \mathrm{~B}_{1} \rightarrow{ }^{2} \mathrm{~A}_{1}$ excitation energy in ${ }^{\circ} \mathrm{NH}_{2}$. As shown schematically in Figure 2, in both of these electronic transitions one electron is excited from a lone pair orbital into a $2 \mathrm{p} \pi$ orbital. At the geometry of the ${ }^{3} \Sigma^{-}$state of NH, CISD/6-311G(2d,p) calculations place ${ }^{3} \Pi 89 \mathrm{kcal} / \mathrm{mol}$ higher in energy than ${ }^{3} \Sigma^{-}$; whereas, at the geometry of the ${ }^{2} \mathrm{~B}_{1}$ state of ${ }^{\bullet} \mathrm{NH}_{2},{ }^{2} \mathrm{~A}_{1}$ is calculated to lie only $52 \mathrm{kcal} / \mathrm{mol}$ above ${ }^{2} \mathrm{~B}_{1}$. The CISD/6-311G(2d,p) difference of $37 \mathrm{kcal} / \mathrm{mol}$ between this pair of excitation energies is very close to the ROHF/6-311G(2d,p) difference of $38 \mathrm{kcal} / \mathrm{mol}$ between the energies of the lone pair orbitals in ${ }^{\circ} \mathrm{NH}_{2}$ and in triplet NH.

Figure 1 shows that the increase in 2 s character, due to rehybridization, also stabilizes the lone pair orbital on formation of ${ }^{\bullet} \mathrm{NH}_{2}$ from $\mathrm{NH}_{3}$. The lowering of the energy of the MO that is occupied by the lone pair of electrons in ${ }^{\bullet} \mathrm{NH}_{2}$ acts to stabilize ${ }^{\bullet} \mathrm{NH}_{2}$, relative to ${ }^{\circ} \mathrm{CH}_{3}$, since, like triplet $\mathrm{CH}_{2},{ }^{\circ} \mathrm{CH}_{3}$ lacks a lone pair of electrons. The greater stabilization provided by rehybridization in ${ }^{\bullet} \mathrm{NH}_{2}$, compared to ${ }^{\circ} \mathrm{CH}_{3}$, provides an explanation for why the $\mathrm{BDEs}^{26}$ of $\mathrm{CH}_{4}(105 \mathrm{kcal} / \mathrm{mol})$ and $\mathrm{NH}_{3}(109 \mathrm{kcal} /$ mol ) are very similar, despite the greater electronegativity of N versus C. ${ }^{27}$

The increase in BDE between $\mathrm{CH}_{4}$ and $\mathrm{NH}_{3}$ is much smaller than the increases between $\mathrm{NH}_{3}, \mathrm{H}_{2} \mathrm{O}(119 \mathrm{kcal} / \mathrm{mol})$, and HF

[^3]( $136 \mathrm{kcal} / \mathrm{mol}$ ). Unlike $\mathrm{CH}_{4}$, the latter three molecules each have a lone pair of electrons that is stabilized by rehybridization in the radical formed by loss of a hydrogen atom. ${ }^{28}$ Therefore, substantial differences in radical rehybridization energies do not act to reduce the effect of the electronegativity of the central atom on the BDEs of $\mathrm{NH}_{3}, \mathrm{H}_{2} \mathrm{O}$, and HF. ${ }^{27}$

## Conclusions

Our computational results demonstrate that triplet nitrenes are generally more thermodynamically stable than comparable triplet carbenes, as evidenced by comparison of the relative enthalpies of nitrenes and carbenes that are isomers (e.g., PhN and $\mathbf{3 - P y C H}$ ) and by comparison of the $\mathrm{X}-\mathrm{H}$ BDEs of RNH and $\mathrm{RCH}_{2}$ radicals. The greater thermodynamic stability of triplet $\mathbf{P h N}$, compared to triplet $\mathbf{P h C H}$, accounts for the much lower reactivity of the former. ${ }^{8}$

Despite the fact that the energy differences between the lowest singlet states of arylnitrenes and arylcarbenes are smaller than those between the triplet ground states, the energy differences between the singlets are still large enough to explain why (a) the ring expansion of singlet $\mathbf{P h N}$ is reversible, ${ }^{2,3}$ whereas that of singlet $\mathbf{P h C H}$ is quite exothermic,, 2 and (b) why singlet pyridyl carbenes (e.g., 2-PyCH and 3-PyCH) rearrange to PhN. ${ }^{9}$ We attribute the greater thermodynamic stability of nitrenes, relative to carbenes, to the presence in the former of a lone pair of electrons which occupies an orbital that is rich in 2 s character.

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Supporting Information Available: Geometries and energies for molecules discussed in this paper (14 pages, print/PDF). See any current masthead page for ordering information and Web access instructions.
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(28) In the second row of the periodic table, the $\mathrm{Si}-\mathrm{H} \mathrm{BDE}$ in $\mathrm{SiH}_{4}$ is also larger than one would expect on the basis of electronegativity; in fact, it is actually larger than the $\mathrm{P}-\mathrm{H}$ BDE in $\mathrm{PH}_{3}$. Again, it is the lone pair in $\mathrm{PH}_{3}$ that causes the $\mathrm{P}-\mathrm{H}$ BDE to be lower than the $\mathrm{Si}-\mathrm{H} \mathrm{BDE}$ of $\mathrm{SiH}_{4}$, but not because of rehybridization of ${ }^{\bullet} \mathrm{PH}_{2}$. Rather, the very large amount of 3 s character already in the lone pair orbital of $\mathrm{PH}_{3}$ results in the $\mathrm{P}-\mathrm{H}$ bonds having much less 3 s character and, hence, being weaker than the $\mathrm{Si}-\mathrm{H}$ bonds in $\mathrm{SiH}_{4}$. [Sun, H.; Hrovat, D. A.; Borden, W. T. J. Am. Chem. Soc. 1987, 109, 5275].


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[^1]:    (23) The values of $23-25 \mathrm{kcal} / \mathrm{mol}$ for the difference between the $\mathrm{N}-\mathrm{H}$ and $\mathbf{C}-\mathrm{H}$ BDEs in forming triplet $\mathbf{P h N}$ from $\mathbf{P h N H}$ and triplet $\mathbf{P h C H}$ from $\mathbf{P h C H}_{2}$ are $10-12 \mathrm{kcal} / \mathrm{mol}$ larger than the ca. $13 \mathrm{kcal} / \mathrm{mol}$ difference between $\Delta E_{\text {ST }}$ in $\mathbf{P h N}$ and $\mathbf{P h C H} .{ }^{1,4-7}$ Therefore, $10-12 \mathrm{kcal} / \mathrm{mol}$ less energy is required to form singlet $\mathbf{P h N}$ from PhNH than to form singlet $\mathbf{P h C H}$ from $\mathbf{P h C H}_{\mathbf{2}}$.
    (24) Ring expansion of singlet 2-PyCH to ACHT is computed to be exothermic by ca. $26 \mathrm{kcal} / \mathrm{mol}$ at the CASPT2N/6-31G* level of theory. The large difference between the energies of the ring expansion reactions of singlet 2-PyCH and singlet $\mathbf{P h N}$ to the same molecule (ACHT) obviously must be due to the higher energy of singlet 2-PyCH, relative to singlet PhN. It should be noted, however, that CASPT2N/6-31G* overestimates the size of the energy difference between singlet 2-PyCH and singlet PhN by ca. $10 \mathrm{kcal} / \mathrm{mol}$, because the CASPT2N value for $\Delta E_{\text {ST }}$ in arylcarbenes is too large by about this amount, but the CASPT2N value for $\Delta E_{\mathrm{ST}}$ in $\mathbf{P h} \mathbf{N}$ is in excellent agreement with experiment. ${ }^{12}$

[^2]:    (25) Rehybridization results in both unpaired electrons occupying pure 2 p orbitals in triplet NH ; whereas, in triplet $\mathrm{CH}_{2}$ one unpaired electron occupies an orbital with substantial amounts of 2 s character. A simplistic argument, based on this difference in hybridization, predicts that a $\mathrm{C}-\mathrm{H}$ bond formed by triplet $\mathrm{CH}_{2}$ should indeed be stronger than an $\mathrm{N}-\mathrm{H}$ bond formed by triplet NH.

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